

L4 - 1.4 - Transformations Lesson

MHF4U

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In this section, you will investigate the roles of the parameters a , k , d , and c in polynomial functions of the form $f(x) = a[k(x - d)]^n + c$. You will apply transformations to the graphs of basic power functions to sketch the graph of its transformed function.

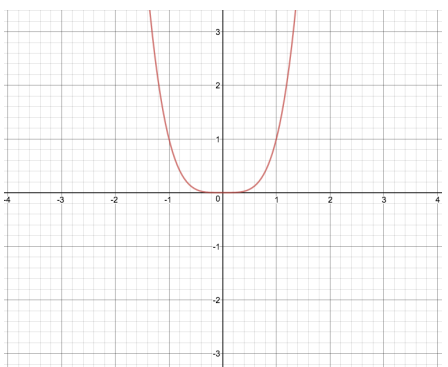
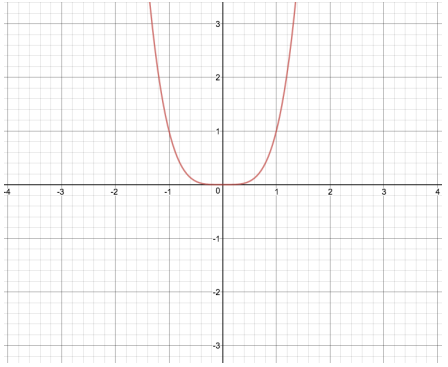
Part 1: Transformations Investigation

In this investigation, you will be looking at transformations of the power function $y = x^4$. Complete the following table using graphing technology to help. The graph of $y = x^4$ is given on each set of axes; sketch the graph of the transformed function on the same set of axes. Then comment on how the value of the parameter a , k , d , or c transforms the parent function.

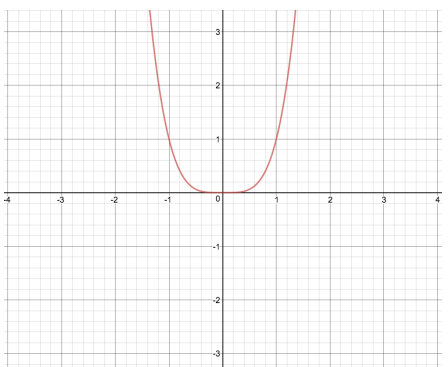
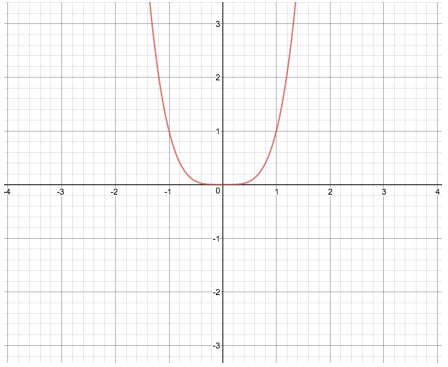
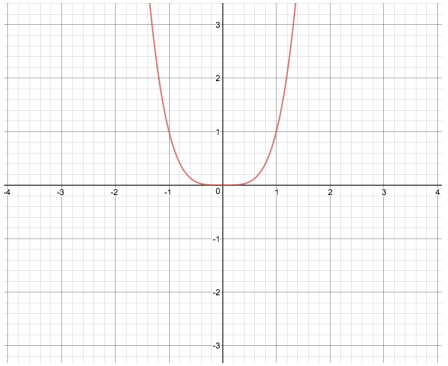
Effects of c on $y = x^4 + c$

Transformed Function	Value of c	Transformations to $y = x^4$	Graph of transformed function compared to $y = x^4$
$y = x^4 + 1$			
$y = x^4 - 2$			

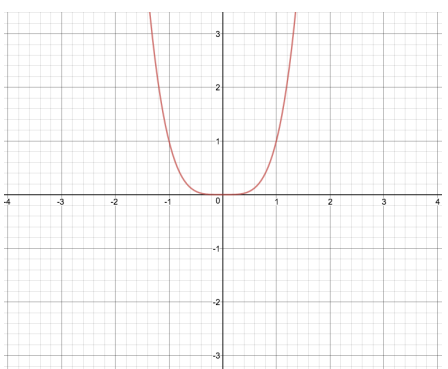
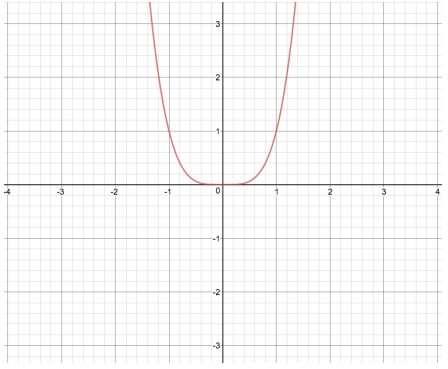
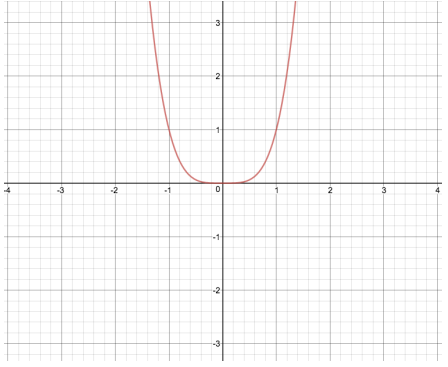
Effects of d on $y = (x - d)^4$

Transformed Function	Value of d	Transformations to $y = x^4$	Graph of transformed function compared to $y = x^4$
$y = (x - 2)^4$			
$y = (x + 3)^4$			

Effects of a on $y = ax^4$

Transformed Function	Value of a	Transformations to $y = x^4$	Graph of transformed function compared to $y = x^4$
$y = 2x^4$			
$y = \frac{1}{2}x^4$			
$y = -2x^4$			

Effects of k on $y = (kx)^4$

Transformed Function	Value of k	Transformations to $y = x^4$	Graph of transformed function compared to $y = x^4$
$y = (2x)^4$			
$y = \left(\frac{1}{3}x\right)^4$			
$y = (-2x)^4$			

Summary of effects of a , k , d , and c in polynomial functions of the form $f(x) = a[k(x - d)]^n + c$

Value of c in $f(x) = a[k(x - d)]^n + c$	
$c > 0$	
$c < 0$	

Value of d in $f(x) = a[k(x - d)]^n + c$	
$d > 0$	
$d < 0$	

Value of a in $f(x) = a[k(x - d)]^n + c$	
$a > 1$ or $a < -1$	
$-1 < a < 1$	
$a < 0$	

Value of k in $f(x) = a[k(x - d)]^n + c$	
$k > 1$ or $k < -1$	
$-1 < k < 1$	
$k < 0$	

Note:

a and c cause _____ transformations and therefore effect the y -coordinates of the function.

k and d cause _____ transformations and therefore effect the x -coordinates of the function.

When applying transformations to a parent function, make sure to apply the transformations represented by a and k BEFORE the transformations represented by d and c .

Part 2: Describing Transformations from an Equation

Example 1: Describe the transformations that must be applied to the graph of each power function, $f(x)$, to obtain the transformed function, $g(x)$. Then, write the corresponding equation of the transformed function. Then, state the domain and range of the transformed function.

a) $f(x) = x^4, g(x) = 2f\left[\frac{1}{3}(x - 5)\right]$

b) $f(x) = x^5, g(x) = \frac{1}{4}f[-2(x - 3)] + 4$

Part 3: Applying Transformations to Sketch a Graph

Example 2: The graph of $f(x) = x^3$ is transformed to obtain the graph of $g(x) = 3[-2(x + 1)]^3 + 5$.

a) State the parameters and describe the corresponding transformations

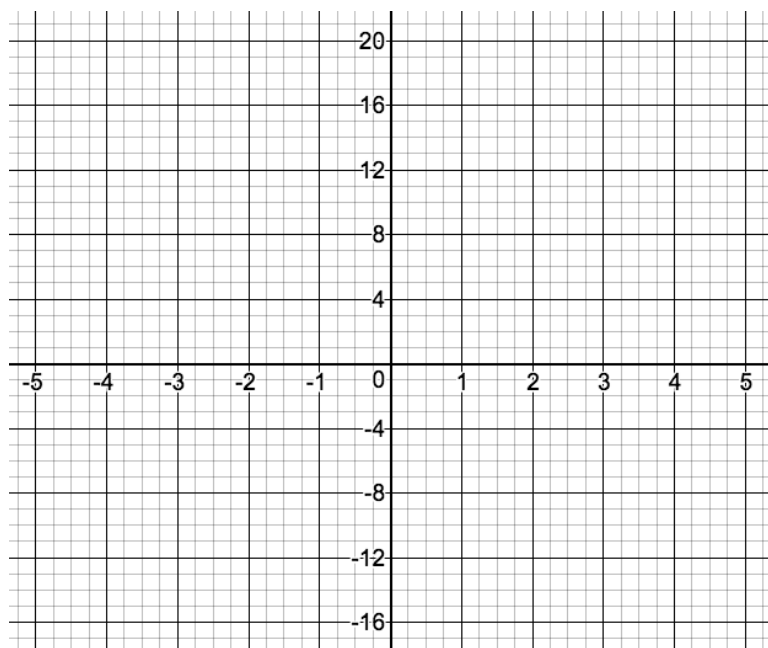
b) Make a table of values for the parent function and then use the transformations described in part a) to make a table of values for the transformed function.

$f(x) = x^3$	
x	y



Note: When choosing key points for the parent function, always choose x -values between -2 and 2 and calculate the corresponding values of y .

c) Graph the parent function and the transformed function on the same grid.



Example 3: The graph of $f(x) = x^4$ is transformed to obtain the graph of $g(x) = -\left(\frac{1}{3}x + 2\right)^4 - 1$.

a) State the parameters and describe the corresponding transformations

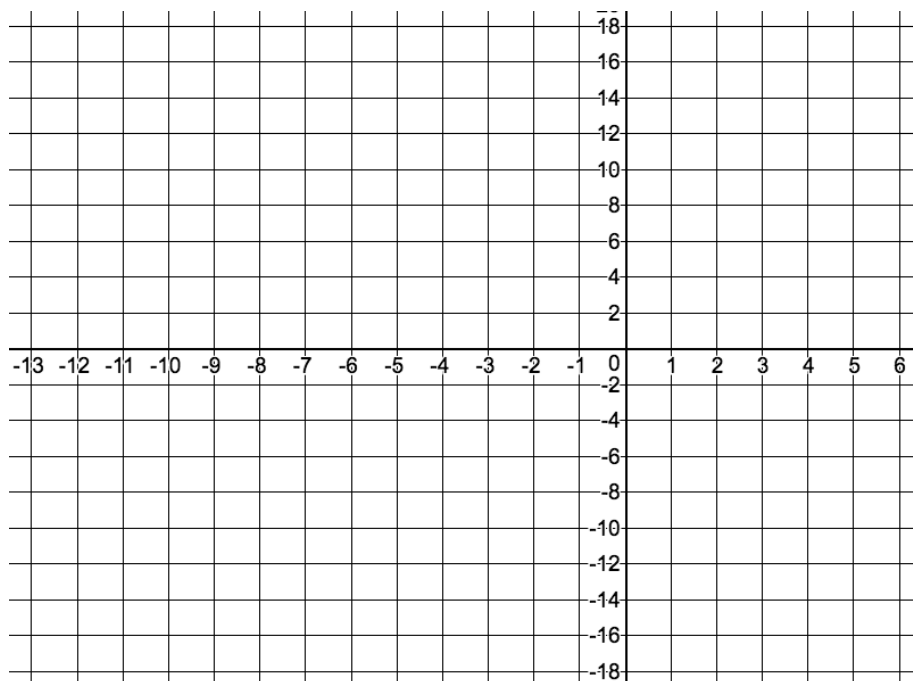
Note: k value must be factored out in to the form $[k(x + d)]$

b) Make a table of values for the parent function and then use the transformations described in part a) to make a table of values for the transformed function.

$f(x) = x^4$	
x	y

→

c) Graph the parent function and the transformed function on the same grid.



Part 4: Determining an Equation Given the Graph of a Transformed Function

Example 4: Transformations are applied to each power function to obtain the resulting graph. Determine an equation for the transformed function. Then state the domain and range of the transformed function.

