

Factoring  $ax^2+bx+c$  if 'a' is not 1 and can't be factored out

1. Check for a common factor
2. Multiply 'a' by 'c'
3. Find two integers who have a product of this number (a x c) and a sum of 'b'
4. Break up the middle term into the integers that satisfy the product and sum
5. Factor by grouping

Factoring  $ax^2+bx+c$  if 'a' is 1 or can be factored out

1. Check for a common factor
2. Find two integers who have a product of 'c' and a sum of 'b'
3. Put those integers into (x+r)(x+s) for 'r' and 's'

Completing the Square:

Going from standard form to vertex form

$$y=ax^2+bx+c \quad \text{to} \quad y=a(x-h)^2+k$$

- 1) Put brackets around the first two terms
- 2) Factor out the number in front of the  $x^2$  (not the letter)
- 3) Look at the last term in the brackets, divide it by 2 and then square it.
- 4) Add and subtract that term behind the last term in the brackets.
- 5) Move the negative term outside of the brackets by first multiplying it by the 'a' value.
- 6) Simplify the terms outside of the brackets.
- 7) Factor the perfect square trinomial  $(x + b/2)^2$

**Perfect Square Trinomial:**

$$a^2+2ab+b^2 = (a+b)^2$$
$$a^2-2ab+b^2 = (a-b)^2$$

**Remember:** the 'c' value of a perfect

square trinomial is half of the 'b' value squared :  $(b/2)^2$

# Chapter 6

## Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Axis of symmetry:  $-b/2a$

Use the discriminant to determine the number of roots:

- If  $b^2-4ac < 0 \rightarrow$  0 roots
- If  $b^2-4ac = 0 \rightarrow$  1 root
- If  $b^2-4ac > 0 \rightarrow$  2 roots

## Solving by Factoring:

- 1) It must be set to equal 0. Before factoring, it must be in the form  $ax^2+bx+c=0$
- 2) Factor the left side of the equation
- 3) Set each factor to equal zero and solve for 'x'.

**zero product rule:** if two factors have a product of zero; one or both of the factors must equal zero.

**Remember:** the axis of symmetry is the x-coordinate of the vertex. Find the axis of symmetry by adding the x-intercepts and then dividing by 2. Use the axis of symmetry to find the y-coordinate of the vertex