

**W2 – The Product Rule**

MCV4U

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Unit 1

**1) Use the product rule to differentiate each function**

**a)**  $f(x) = (5x + 2)(8x - 6)$

**b)**  $h(t) = (-t + 4)(2t + 1)$

**c)**  $p(x) = (-2x + 3)(x - 9)$

**d)**  $g(x) = (x^2 + 2)(4x - 5)$

**e)**  $f(x) = (1 - x)(x^2 - 5)$

**f)**  $h(t) = (t^2 + 3)(3t^2 - 7)$

**2)** Determine  $f'(-2)$  for each function.

**a)**  $f(x) = (x^2 - 2x)(3x + 1)$

**b)**  $f(x) = (1 - x^3)(-x^2 + 2)$

**3)** Determine an equation for the tangent to each curve at the indicated value.

**a)**  $f(x) = (x^2 - 3)(x^2 + 1)$  at  $x = -4$

**b)**  $h(x) = (x^4 + 4)(2x^2 - 6)$  at  $x = -1$

**4)** Determine the point(s) on each curve that correspond to the given slope of the tangent.

**a)**  $y = (-4x + 3)(x + 3), m = 0$

**b)**  $y = (x^2 - 2)(2x + 1), m = -2$

**5)** Differentiate using the product rule.

**a)**  $y = (5x^2 - x + 1)(x + 2)$

**b)**  $y = -x^2(4x - 1)(x^3 + 2x + 3)$

**6)** The owner of a local hair salon is planning to raise the price for a haircut and blow dry. The current rate is \$30 for this service, with the salon averaging 550 clients a month. A survey indicates that the salon will lose 5 clients for every incremental price increase of \$2.50.

**a)** Write an equation to model the salon's monthly revenue,  $R$ , in dollars, as a function of  $x$ , where  $x$  represents the number of \$2.50 increases in the price.

**b)** Use the product rule to determine  $R'(x)$

**c)** Evaluate  $R'(3)$  and interpret it for this situation.

**d)** Solve  $R'(x) = 0$ .

**e)** Explain how the owner can use the result of part d).

**Answers:**

**1)a)**  $f'(x) = 80x - 14$  **b)**  $h'(t) = -4t + 7$  **c)**  $p'(x) = -4x + 21$  **d)**  $g'(x) = 12x^2 - 10x + 8$

**e)**  $f'(x) = -3x^2 + 2x + 5$  **f)**  $h'(t) = 12t^3 + 4t$

**2)a)** 54 **b)** 60

**3)a)**  $y = -240x - 739$  **b)**  $y = -4x - 24$

**4)a)**  $\left(-\frac{9}{8}, \frac{225}{16}\right)$  **b)** (0.43, -3.38) and (-0.77, 0.76)

**5)a)**  $15x^2 + 18x - 1$  **b)**  $-24x^5 + 5x^4 - 32x^3 - 30x^2 + 6x$

**6)a)**  $R(x) = (30 + 2.50x)(550 - 5x)$  **b)**  $R'(x) = 1225 - 25x$  **c)** 1150; this is the rate of change of revenue at a \$7.50 increase **d)**  $x = 49$  **e)** The owner could maximize the revenue by making 49 increases of \$2.50. A visit to the hair salon would cost \$152.50 and would generate a max revenue of \$46 512.50.