

W3 – Applications of the Dot Product

Unit 5

MCV4U

Jensen

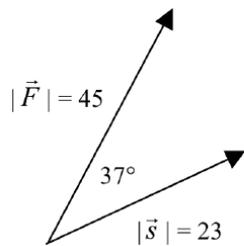
1) Determine the work done by each force \vec{F} , in Joules, for each object moving along \vec{s} .

a) $\vec{F} = [3, -2]$, $\vec{s} = [1, 8]$

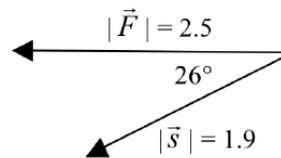
b) $\vec{F} = [8, -9]$, $\vec{s} = [-3, 7]$

2) Determine the work done by the force \vec{F} , in Joules, for each object moving along \vec{s} .

a)



b)



3) Determine the angle between the vectors in each pair.

a) $\vec{p} = [6, 7]$ and $\vec{q} = [3, 2]$

b) $\vec{r} = [-1, -7]$ and $\vec{s} = [5, 4]$

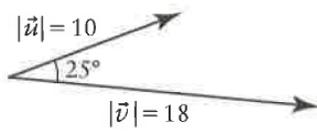
4) Determine the projection of the first vector on the second.

a) $\vec{a} = [6, -1]$, $\vec{b} = [3, -4]$

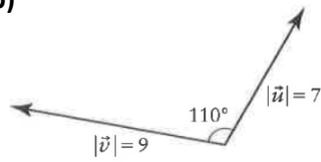
b) $\vec{c} = [6, 7]$, $\vec{d} = [3, 2]$

5) Determine the projection of \vec{u} on \vec{v}

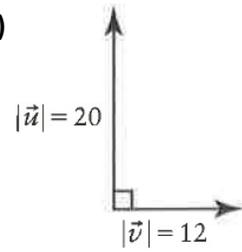
a)



b)



c)



6) For each of the following, find the magnitude of the projection of \vec{x} on \vec{y} and also the vector projection of \vec{x} on \vec{y} .

a) $\vec{x} = [1,1], \vec{y} = [1, -1]$

b) $\vec{x} = [2,5], \vec{y} = [-5,12]$

7) $\triangle DEF$ has vertices $D(-3, 5)$, $E(2, 3)$, and $F(6, 7)$. Calculate $\angle DEF$.

- 8) How much work is done against gravity by the orderly pushing an 85 kg person up a 5 m ramp inclined at an angle of 15° to the horizontal?
- 9) A stage lamp is dragged 15 m along level ground by a 120 N force applied at an angle of 35° to the ground. It is then dragged up a 12m ramp, inclined at 15° to the ground, onto a stage using the same force. Find the total work done.
- 10) A box on a wagon pulled a distance of 35 m by a 27 N force applied at an angle of 40° to the ground. The box is then lifted a distance of 1.5 m and placed on a table by exerting a force of 37 N. Find the total work done.

ANSWER KEY

1)a) -13 b) -87

2)a) 826.59 b) 4.27

3)a) $\theta = 15.71^\circ$ b) $\theta = 136.79^\circ$

4)a) $\left[\frac{66}{25}, -\frac{88}{25}\right]$ b) $\left[\frac{96}{13}, \frac{64}{13}\right]$

5)a) $9.06\hat{i}$ b) $-2.39\hat{i}$ c) $\vec{0}$

6) magnitude = 0, vector projection: $\vec{0}$ b) magnitude = $\frac{50}{13}$, vector projection: $\left[\frac{-250}{169}, \frac{600}{169}\right]$

7) 113.2°

8) 1077.98 J

9) 2827.63 J

10) 779.4 J